









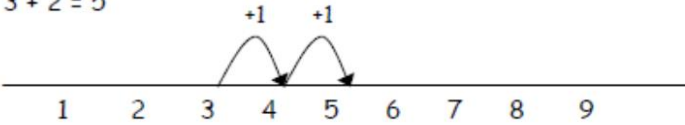
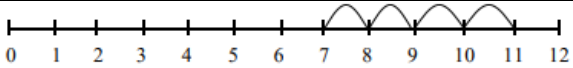
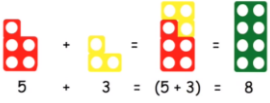

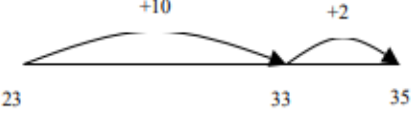
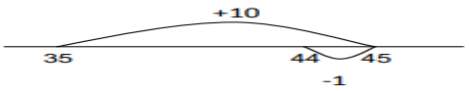



Ysgol
Bro
Dyfrdwy
Calculation
Methods

Progression Step 1 - 3-5years
 Progression Step 2 - 6-8years
 Progression Step 3 - 9-11years
 Progression Step 4 - 11+years



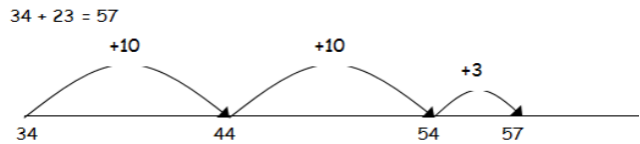
Addition Steps

<p>Progression Step 1</p>	<p>Identify and name numbers from 0 -10</p> 	
	<p>Count objects one by one to 10 and beyond.</p> 	
	<p>Use fingers to count from 1-10. Start with little finger as 1 and 6.</p> 	
	<p>Count sets of objects and develop ways to record numbers in a range of ways e.g dots, pictures words or symbols.</p>	

	<p>Use a number line to 10 to count one by one.</p> 	<p>$3 + 2 = 5$</p> 
	<p>Use a number line to 20 to count one by one. E.g $7 + 4 =$</p>	
	<p>Use numicon</p>	 <p>$5 + 3 = (5+3) = 8$</p>
	<p>$8 + 7 = 15$ First add 2 to make 10 and then add 5 to make 15.</p>	
	<p>Use a number line to count onwards in tens and ones. First of all jump 10 then 2 $23 + 12 = 35$</p>	
	<p>Add 9 or 11 and adjust 1</p>	<p>$35 + 9 = 44$</p> 
	<p>Identify number bonds to 20 in your head.</p>	<p>$5 + 2 = 7$ $15 + 2 = 17$ $50 + 20 = 70$</p>
<p>Progression step 2</p>	<p>Partition tens and units 29 $20 + 9$</p> 	<p>$29 = 20 + 9$</p> <p>Tens 20 = Tap the chest twice </p>  <p>Units = 9</p>

Partition tens and units
(ones)

$$34 + 23 = 57$$

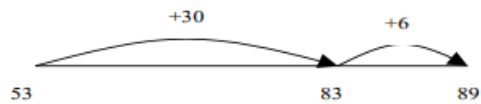


Partition tens and units

$$36 + 53 =$$

$$53 + 30 + 6 =$$

$$83 + 6 = 89$$



$$37 + 15 =$$



Add the tens

$$30 + 10 = 40$$

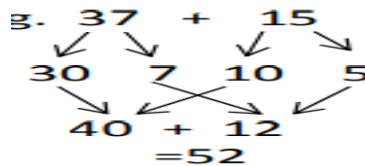
Add the units

$$7 + 5 = 12$$

Add the tens and units

$$40 + 12 = 52$$

Partition tens and units
using the diamond.



Vertical addition

Ensure understanding of
place value. Start with
adding the units.



$$\begin{array}{r} 346 \\ + 273 \\ \hline 9 \\ 110 \\ \hline 500 \end{array}$$

Once understood the
previous method. Start
counting from the units.
Carry over if needed.

$$\begin{array}{r} 3464 \\ + 2739 \\ \hline 6203 \\ \hline 111 \end{array}$$

Progression step

3

Decimal addition



$$\begin{array}{r} 23.56 \\ + 19.75 \\ \hline 43.31 \\ \text{1 1 1} \end{array}$$



Subtraction Steps

Progression
Steps 1

Count back one by one from 10 - 0



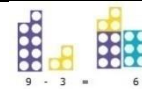
Count sets of objects and develop ways to record numbers in a range of ways e.g dots, pictures words or symbols.



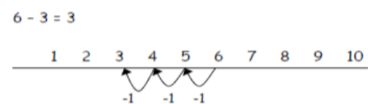
Use your fingers to subtract to 10. Start with little finger as 1 and 6.



Use numicon



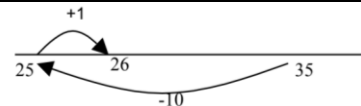
Use number line to 10 to count back one by one.



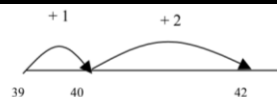
Count back on a number line over 10.
 $11 - 5 =$



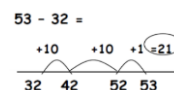
Subtract 9 or 11 and adjust 1
 $35 - 9 = 26$

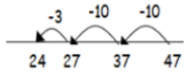
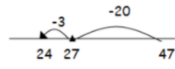

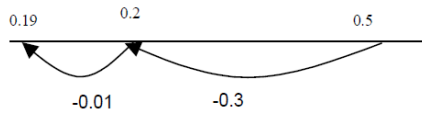


Use a number line to count forwards to discover the difference.
 $42 - 39 = 3$



Discover the difference by counting forwards..



	$53 - 32 = 21$	
Progression Steps 2	<p>Discover the difference by subtracting and counting backwards in steps..</p> $47 - 23 = 24$	
	<p>Discover the difference by subtracting and counting backwards in steps of tens.</p> $47 - 23 = 24$	<p>$47 - 23 = 24$</p> 
	<p>Traditional method, ensure largest number on top, subtracting starting with the units.</p> 	$\begin{array}{r} 28 \\ - 5 \\ \hline 23 \end{array}$
	<p>Ensure largest number on top. Borrow ten from previous column when not possible to complete the calculation. Subtract starting with the units.</p>	$\begin{array}{r} 6 \ 14 \ 1 \\ \cancel{7} \ 5 \ 4 \\ - 2 \ 9 \ 7 \\ \hline 4 \ 5 \ 7 \end{array}$
Progression Step 3	<p>Use knowledge of number bonds and place value to subtract. (count back)</p>	<p>$0.5 - 0.31 = 0.19$</p> 

Subtract decimals as 'bunk beds' when dealing with larger numbers.

Remember to keep the decimal point in the same place. Always start from the units.



$$\begin{array}{r} 0\ 1\ 5\ 1 \\ \cancel{1}7\cancel{6} . 48 \\ \underline{93 . 72} \\ 82 . 76 \end{array}$$



Multiplication steps

Progression step
2

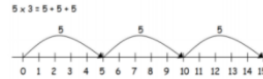
Count every 2,5, or 10.
Recognise doubles to 5



Count sets of objects.



Count every 2 e.g count legs, socks, eyes
Count every 5 e.e fingers
Count every 10 e.e count hands



Draw pictures / markings



There are 3 sweets in 1 bag. How many sweets are there in 5 bags?

Recognise doubles to 20

$$5 \times 2 = 10$$

$$10 \times 2 = 20$$

Progression step 2

Use multiplication 2,3,4,5
and 10

Introduce that multiplication is repetitive addition.

4×2 or $4 + 4$
 2×4 or $2 + 2 + 2 + 2$



Use symbols = and x to complete number sentences.

$$10 \times 5 = \underline{\quad}$$

$$8 \times \underline{\quad} = 16$$

$$\begin{array}{r} \times 10 \quad 5 \\ 2 \quad 20 \quad 10 \quad = 30 \end{array}$$

$$15 \times 2 = 30$$

	<p>Grid method to partition tens and units.</p>							
<p>Progression step 3</p>	<p>Grid method - partition 2 digit numbers.</p> 	<p>ee. 57×45</p> $\begin{array}{r} \times \quad) \qquad \qquad \qquad 7 \\ 40 \end{array}$ <table border="1" data-bbox="896 504 1334 712"> <tr> <td>2000</td> <td>280</td> <td>=2280</td> </tr> <tr> <td>250</td> <td>35</td> <td>= 285</td> </tr> </table> <p>5</p> <p style="text-align: right;">2565</p>	2000	280	=2280	250	35	= 285
2000	280	=2280						
250	35	= 285						
	<p><u>Column method</u></p> <p>Partition numbers into tens and units. (2 digit x 1 digit)</p>  <p><u>Column method</u></p> <p>Partition numbers into tens and units. (2 digit x 2 digit)</p>	<p>$38 \times 5 =$</p> $\begin{array}{r} 38 \\ \times 5 \\ \hline 40 \quad (5 \times 8) \\ 150 \quad (5 \times 30) \\ \hline 190 \end{array}$ <p>$38 \times 14 =$</p> $\begin{array}{r} 38 \\ \times 14 \\ \hline 32 \quad (4 \times 8) \\ 120 \quad (4 \times 30) \\ 80 \quad (10 \times 8) \\ \underline{300} \quad (10 \times 30) \\ \hline 532 \\ \color{red}{1} \end{array}$						

Napier rods method

Another grid method, but this time divide the boxes diagonally to enable you to multiply digits individually (tens on the top and units on the bottom).

Then add the diagonal columns to reach the final answer.



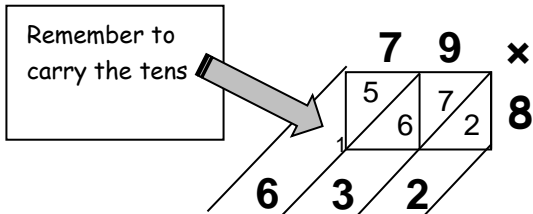
2 x 1 digit



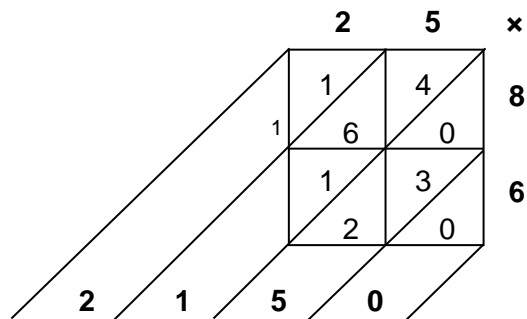
2 x 2 digits

Multiply with single number

e.g $79 \times 8 = 632$



e.g $25 \times 86 = 2150$



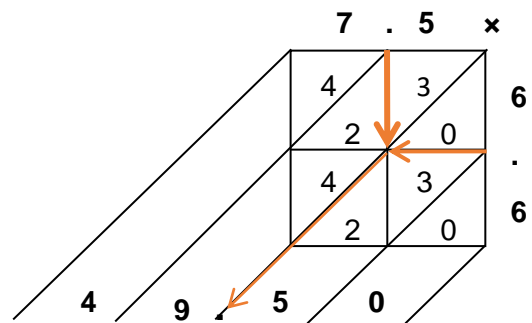
Napier rods method

Multiply with decimals.

Ensure the decimal point is moved using the red arrows as a guide.








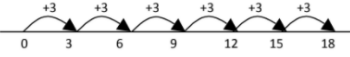



$7.5 \times 6.6 = 49.5$





Division Progression steps

Progression step 1	Divide objects equally.	E.g share the milk bottles, share pencils or share fruit. 
	Count every 2,5 and 10.	
	Count confidently to share objects correctly. 	 Share 6 sweets with 2 people.
	Group objects into sets of 2, 5 or 10.	 How many pair of socks are there? 
Progression step 2 Use multiplication 2,3,4,5 and 10	Group numbers whilst jumping on the number line. 	How many groups of 3 in 18? 
	Use the symbols = and ÷ to complete number sentences.	$10 \div 5 = \underline{\quad}$ $8 \div \underline{\quad} = 4$
	<u>Chunking division while subtracting</u> Subtract familiar multiples in steps and then add the amount.	e.g $155 \div 5 = 31$ $\begin{array}{r} 31 \\ 5 \overline{)155} \\ \underline{-150} \quad (30 \times 5) \\ 5 \end{array}$

		$5 \quad (1 \times 5)$
	<p><u>Chunking division while subtracting</u></p> <p>Subtract familiar multiples in steps and then add the amount and remember the remainder.</p>	<p>eg. $235 \div 7 =$</p> $ \begin{array}{r} 33 \text{ r}4 \\ 7 \overline{)235} \\ \underline{-70} \quad (10 \times 7) \\ 165 \\ \underline{-70} \quad (10 \times 7) \\ 95 \\ \underline{-70} \quad (10 \times 7) \\ 25 \\ \underline{-21} \quad (3 \times 7) \\ 4 \end{array} $ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin-left: auto;"> <p>7 into 235, 33 times with a remainder of 4.</p> </div>
<p>Progression step 3</p>	<p><u>Short division method</u></p> <p>Use multiplication knowledge to divide numbers into specific numbers.</p> 	<p>eg. $57 \div 3 = 19$</p> $ \begin{array}{r} 19 \\ 3 \overline{)57} \\ \underline{3} \quad (3 \times 1 = 3) \\ 27 \\ \underline{27} \\ 0 \end{array} $ <p>2 remainder</p>

